

## Supplementary Material

	Plate positioning	Plate deformation	Fit criteria	Plate set	Surgery ready	Anatomic constraints
2007 Goyal	x	x	x	x	x	x
2008 Schmutz	x	NA	o	x	x	x
2010 Kozic	o	x	o	x	x	x
2011 Schmutz	x	x	o	o	x	x
2011 Bou-Sleiman	NA	o	x	x	x	x
2012 Schulz	NA	x	o	x	x	x
2016 Harith	o	x	o	o	x	x
2018 Petersik	o	x	x	x	x	x
2019 Schmutz	x	x	o	x	x	x
2019 Wu	x	NA	o	x	x	x
2019 Tkany	o	x	o	x	x	x
2022 Zenker	NA	x	x	x	x	x
Ours	o	o	o	o	o	o

Table 1: Comparative table of plate designs and evaluation methods. Legend: (o: yes); (x: no), (NA: non-available or non-applicable). “Plate positioning” and “Plate deformation”: is it done automatically? Fit criteria: is there a binary fit criterion? Plate set: does the method provide several plates? Surgery ready: given a bone, does the method provide a surgery-ready plate shape? Anatomic constraints: does the plate positioning optimization consider anatomic constraints?

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### Algorithm 1 Plate set creation algorithm.

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1: procedure BUILDPLATESET(plate_list plate_list, bone_list bone_list)
2:   plate_set  $\leftarrow \emptyset$ 
3:   while |bone_list|  $\geq 0$  do
4:     plate_sorted  $\leftarrow \text{sort.by.bone.fit.nb}(\text{plate.list}, \text{bone.list})$ 
5:     plate  $\leftarrow \text{plate.sorted.pop}(0)$ 
6:     plate_set.append(plate)
7:     for bone  $\in \text{fit.bone.list}(\text{plate}, \text{bone.list})$  do
8:       bone_list.remove(bone)
9:     end for
10:  end while
11:  return plate_set
12: end procedure

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## Plate positioning

### Definitions:

- B**: the input bone mesh.  
 **$\mathcal{B}_h$** : the vertices on the head fixation region of the bone.  
 **$\mathcal{B}_s$** : the vertices on the side fixation region of the bone.  
**P**: the input plate mesh.  
 **$N_p$** : number of vertices of the plate mesh.  
 **$\mathbf{r} \in \mathbb{R}^{3 \times 3}$** : a 3D rotation.  
 **$\mathbf{t} \in \mathbb{R}^3$** : a 3D translation.  
 **$\mathbf{P}^{\mathbf{r}, \mathbf{t}} = \mathbf{r} \cdot \mathbf{P} + \mathbf{t}$** : the positioned plate.  
 **$\mathcal{P}_h^{\mathbf{r}, \mathbf{t}}$** : the vertices on the head fixation region of the positioned plate.  
 **$\mathcal{P}_s^{\mathbf{r}, \mathbf{t}}$** : the vertices on the side fixation region of the positioned plate.

- $d(\cdot, \cdot) \rightarrow \mathbb{R}$** : the Chamfer distance between two point sets.  
 **$col(A, B) \rightarrow \mathbb{N}$** : counts the number of vertices of  $A$  which are inside  $B$ .

- $w_i$** : optimization weights:  $w_1 = 5, w_2 = 0.01$ .  
 **$d_c = 0.01$  mm**: collision threshold.  
 **$d_s = 2$  mm**: snap threshold.  
 **$\alpha = 16$** : constant.

- $\mathbf{r}_0, \mathbf{t}_0$**  Initial position of the plate.  
 **$\mathbf{r}_f, \mathbf{t}_f$**  Final position of the plate.

### Equations:

$$\arg \min_{\mathbf{r}_0, \mathbf{t}_0} E_1(\mathbf{r}, \mathbf{t}; \mathbf{P}, \mathbf{B}) = w_1 d(\mathcal{P}_h^{\mathbf{r}, \mathbf{t}}, \mathcal{B}_h) + d(\mathcal{P}_s^{\mathbf{r}, \mathbf{t}}, \mathcal{B}_s). \quad (1)$$

$$\begin{aligned} \arg \min_{\mathbf{r}_f, \mathbf{t}_f} E_2(\mathbf{r}, \mathbf{t}; \mathbf{P}, \mathbf{B}) = w_2 \, & col(\mathbf{P}^{\mathbf{r}, \mathbf{t}}, \mathbf{B}) \, E_{col}(\mathbf{P}^{\mathbf{r}, \mathbf{t}}, \mathbf{B}) \\ & + E_{snap}(\mathcal{P}_h^{\mathbf{r}, \mathbf{t}}, \mathcal{B}_h) \\ & + E_{snap}(\mathcal{P}_s^{\mathbf{r}, \mathbf{t}}, \mathcal{B}_s) \end{aligned} \quad (2)$$

where

$$E_{col}(\mathbf{P}, \mathbf{B}) = \sum_{i \in [1, N_p]} \begin{cases} (E_{p2m}(\mathbf{p}_i, \mathbf{B}) - d_c)^2 + \sigma(d_c), & \text{if } E_{p2m}(\mathbf{p}_i, \mathbf{B}) \leq d_c \\ \sigma(E_{p2m}(\mathbf{p}_i, \mathbf{B})), & \text{if } E_{p2m}(\mathbf{p}_i, \mathbf{B}) > d_c \end{cases} \quad (3)$$

with

$$\sigma(x) = \frac{1}{1 + e^{-\alpha(x-d_c)}} \quad (4)$$

and

$$E_{snap}(\mathbf{P}, \mathbf{B}) = \sum_{i \in [1, N_p]} \begin{cases} 0, & \text{if } E_{p2m}(\mathbf{p}_i, \mathbf{B}) \leq d_s \\ (E_{p2m}(\mathbf{p}_i, \mathbf{B}) - d_s)^2, & \text{if } E_{p2m}(\mathbf{p}_i, \mathbf{B}) > d_s. \end{cases} \quad (5)$$